

# Lesson 5.3 Properties of Operations

Objective: To identify and use mathematical properties to simplify algebraic expressions

## Properties of Operations

**Words** The **Commutative Property** states that the order in which numbers are added or multiplied does not change the sum or product.

	Addition	Multiplication
<b>Symbols</b>	$a + b = b + a$	$a \cdot b = b \cdot a$
<b>Examples</b>	$6 + 1 = 1 + 6$	$7 \cdot 3 = 3 \cdot 7$

**Words** The **Associative Property** states that the way in which numbers are grouped when they are added or multiplied does not change the sum or product.

	Addition	Multiplication
<b>Symbols</b>	$a + (b + c) = (a + b) + c$	$a \cdot (b \cdot c) = (a \cdot b) \cdot c$
<b>Examples</b>	$2 + (3 + 8) = (2 + 3) + 8$	$3 \cdot (4 \cdot 5) = (3 \cdot 4) \cdot 5$

A **property** is a statement that is true for any number. The following properties are also true for any numbers.

Property	Words	Symbols	Examples
<b>Additive Identity</b>	When 0 is added to any number, the sum is the number.	$a + 0 = a$ $0 + a = a$	$9 + 0 = 9$ $0 + 9 = 9$
<b>Multiplicative Identity</b>	When any number is multiplied by 1, the product is the number.	$a \cdot 1 = a$ $1 \cdot a = a$	$5 \cdot 1 = 5$ $1 \cdot 5 = 5$
<b>Multiplicative Property of Zero</b>	When any number is multiplied by 0, the product is 0.	$a \cdot 0 = 0$ $0 \cdot a = 0$	$8 \cdot 0 = 0$ $0 \cdot 8 = 0$

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Ex. 1 Name the property shown by the statement.

$$2 \cdot (5 \cdot n) = (2 \cdot 5) \cdot n$$

Associative property of Multiplication

Ex. 2 State whether the following conjecture is true or false. If false, provide a counter example.

Division of whole number is commutative.

$$15 \div 3 = 3 \div 15 \quad 15 \overline{)3.0} \quad \frac{0.2}{10} = \frac{2}{10} = \frac{1}{5}$$

$$5 \neq \frac{1}{5}$$

False. We found a counter example that is  $15 \div 3 \neq 3 \div 15$ .

Ex. 3 Simplify each expression. Justify each step.

$$\begin{aligned} (7+g)+5 &= (g+7)+5 && \text{Commutative +} \\ &= g+(7+5) && \text{Associative +} \\ &= g+12 && \text{Simplify} \end{aligned}$$